

# Light Inflation – Reconciling $\phi^4$ Inflation with Planck and Experimental Prospects

F. Bezrukov

University of Connecticut  
&  
RIKEN-BNL Research Center  
USA

Exploring the Physics of Inflation  
Santander, Spain  
June 24–27, 2013

# Outline

- 1 Minimally extending the Standard Model
- 2  $\phi^4$  inflation after Planck
  - Minimally coupled inflation
  - Non-minimally coupled inflation
- 3 Coupling to the SM and cosmological constraints
  - The full model
  - Constraints from reheating and radiative corrections
- 4 Anything interesting in the laboratory?
  - Direct inflaton search
  - Is the Higgs compatible?

# Standard Model of particle physics

Three Generations  
of Matter (Fermions) spin  $\frac{1}{2}$

	I	II	III		
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
name →	<b>u</b> Left up Right	<b>c</b> Left charm Right	<b>t</b> Left top Right	<b>g</b> gluon	
	4.8 MeV	104 MeV	4.2 GeV	0	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	0
Quarks	<b>d</b> Left down Right	<b>s</b> Left strange Right	<b>b</b> Left bottom Right	<b><math>\gamma</math></b> photon	
	0 eV	0 eV	0 eV	91.2 GeV	>114 GeV
	0	0	0	0	0
	<b><math>\nu_e</math></b> Left electron neutrino Right	<b><math>\nu_\mu</math></b> Left muon neutrino Right	<b><math>\nu_\tau</math></b> Left tau neutrino Right	<b>Z<sup>0</sup></b> weak force	<b>H</b> Higgs boson
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV	
	-1	-1	-1	$\pm 1$	
Leptons	<b>e</b> Left electron Right	<b><math>\mu</math></b> Left muon Right	<b><math>\tau</math></b> Left tau Right	<b>W<sup>±</sup></b> weak force	spin 0

Bosons (Forces) spin 1

# Standard Model and nothing else above up to Planck scale?

- No heavy particles/scales
  - no physical high scale quadratic contributions to the Higgs boson mass
  - hierarchy problem is not that scary (however, the gravity should be generous enough not to give quadratically divergent contributions)
  - Processes at the highest energy (inflation) may be directly related to the low energy properties

# Standard Model – extended for inflation

Some models that minimally expand the SM and have inflation

- Higgs inflation
  - very direct relation of inflation and SM, some subtleties with the UV properties
- $R^2$  inflation
  - purely gravitational solution, nothing interesting for the particle physics
- Light inflaton with non-minimal coupling
  - this talk, solution on the particle physics side

Note – the whole Universe evolution should be fully described within the model!

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# “Standard” chaotic inflation

## Scalar part of the action

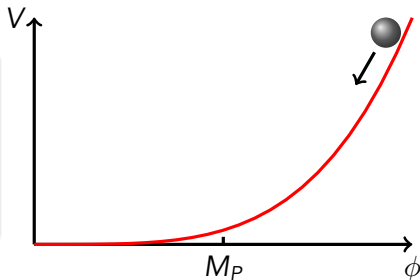
$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\beta}{4} \phi^4 \right\}$$

## Required to get

$$\delta T/T \sim 10^{-5}$$

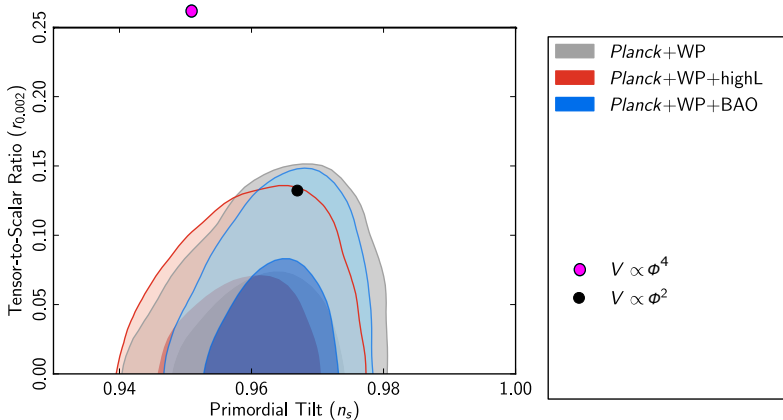
$$\beta \sim 10^{-13}$$

$$m \sim 10^{13} \text{ GeV}$$



Fields  $\gtrsim M_P$ , energy  $\sim \lambda^{1/4} M_P$ .

# Planck results disfavor plain $\phi^4$





# Non-minimal coupling to gravity leads to good inflation

## Scalar action with non-minimal coupling

$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \frac{\xi}{2} \phi^2 R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\lambda}{4} \phi^4 \right\}$$

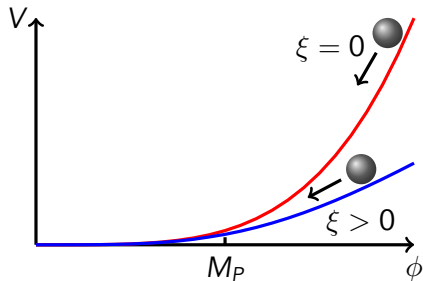
Conformal transformation to the Einstein frame

$$\hat{g}_{\mu\nu} = \sqrt{1 + \frac{\xi \phi^2}{M_P^2}} g_{\mu\nu},$$

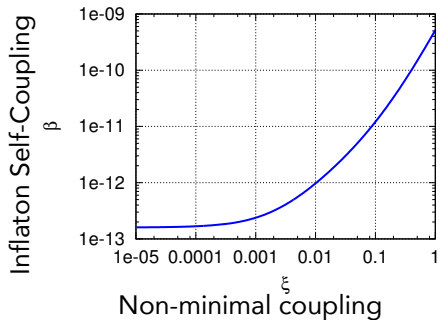
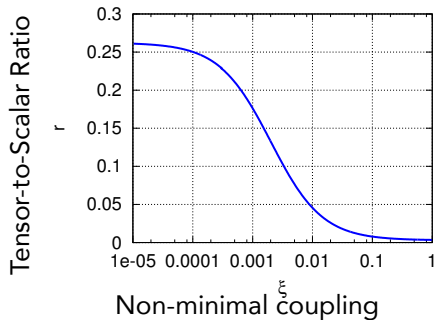
flattens the potential

$$V(\phi) \rightarrow \hat{V}(\phi) = \frac{V(\phi)}{(1 + \xi \phi^2 / M_P^2)^2}$$

(Change of the field  $\frac{d\chi}{d\phi} = \sqrt{\frac{1 + (\xi + 6\xi^2)\phi^2 / M_P^2}{(1 + \xi \phi^2 / M_P^2)^2}}$  is also needed)

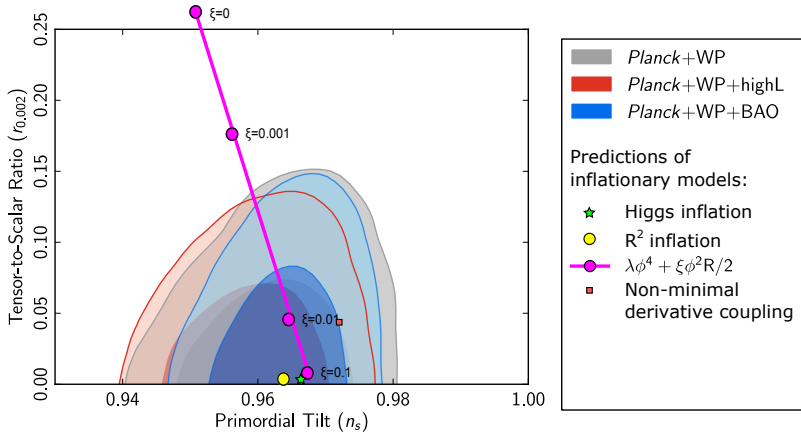


The tensor perturbations are suppressed,  
inflaton self-coupling  $\beta$  is increased



[Tsujiikawa, Gumjudpai'04, FB'08, Okada, Rehman, Shafi'10]

# Inflationary predictions are ok for $\xi \gtrsim 0.003$



# SM + Light Inflaton coupled in the Higgs sector only

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \alpha H^\dagger H \phi^2 + \frac{\beta}{4} \phi^4 + \frac{\xi \phi^2}{2} R$$

Standard Model
Interaction
Inflationary sector

Inflaton mass depends on interaction strength:  $m_\chi = m_h \sqrt{\beta/2\alpha}$

Specifically: the Higgs-inflaton scalar potential is

$$V(H, \phi) = \lambda \left( H^\dagger H - \frac{\alpha}{\lambda} \phi^2 \right)^2 + \frac{\beta}{4} \phi^4 - \frac{1}{2} \mu^2 \phi^2 + V_0$$

We assumed here, that the scale invariance is broken *in the inflaton sector only*

[Shaposhnikov, Tkachev'06, Anisimov, Bartocci, FB'09, FB, Gorbunov'10,13]

# All constants of the model are bound from cosmology

CMB normalization sets  $\beta(\xi)$

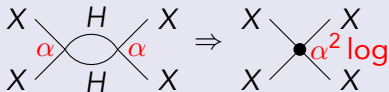
$$\beta = \frac{3\pi^2 \Delta_{\mathcal{R}}^2}{2} \frac{(1+6\xi)(1+6\xi+8(N+1)\xi)}{(1+8(N+1)\xi)(N+1)^3}$$

CMB tensor modes bound  $\xi$

$$r = \frac{16(1+6\xi)}{(N+1)(1+8(N+1)\xi)} \lesssim 0.15$$

$\alpha \lesssim \beta^2$  (mass lower bound)

Inflation is not spoiled by the radiative corrections

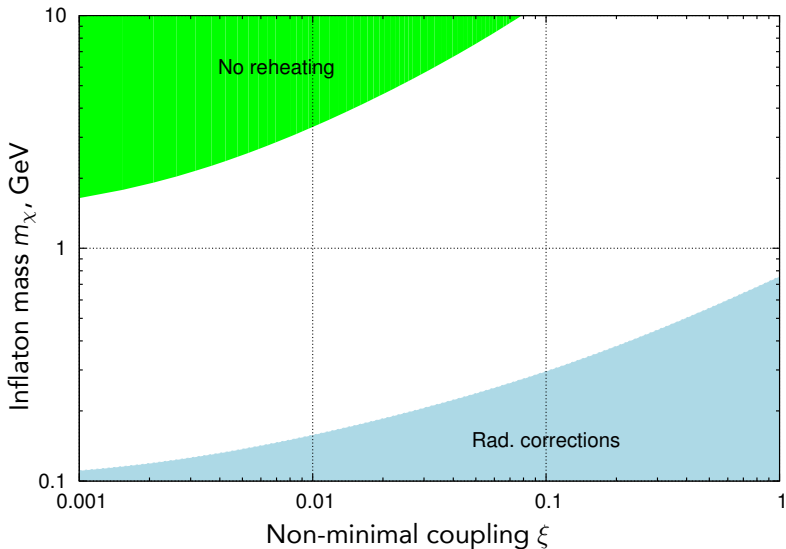


$\alpha > 10^{-7}$  (mass upper bound)

Sufficient reheating

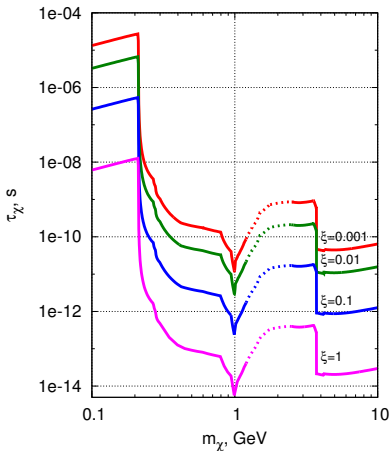
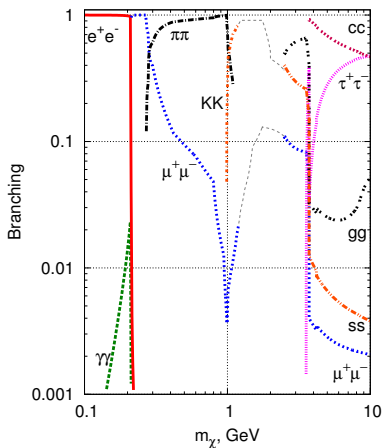
- After inflation: empty & cold
- Needed: hot,  $T_r \gtrsim 150$  GeV (to get baryogenesis)

# The Inflaton mass is bounded from cosmology



# Inflaton decays and lifetime

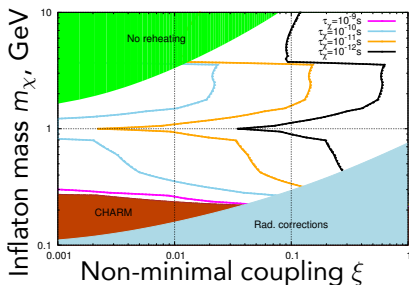
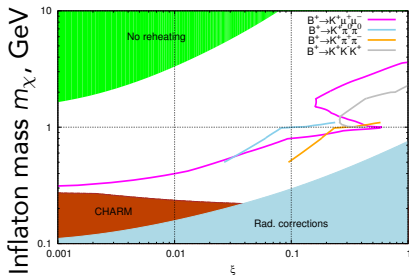
Coupled to everything proportional particle mass



Created in meson decays:

$$\text{Br}(B \rightarrow \chi X_s) \simeq 10^{-6} \frac{\beta(\xi)}{1.5 \times 10^{-13}} \frac{300 \text{ MeV}^2}{m_\chi}$$

# Experimental searches are possible



Behaves as light "Higgs" boson, suppressed by

$$\theta = \sqrt{2\beta}v/m_\chi$$

- Created in meson decays
- Decays:  $KK$ ,  $\pi\pi$ ,  $\mu\mu$ ,  $ee$ , ...
- Interacts with media: extremely weakly

Search (LHCb, Belle)

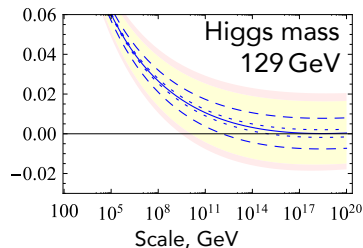
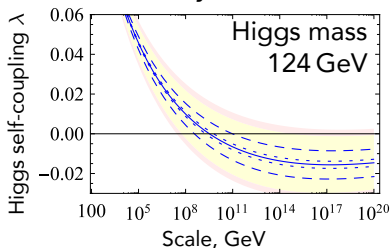
- Events with offset vertices in B decays
- Peaks in Dalitz plot of three body B decays



# Another prediction: The Higgs boson can not be light

Inflation proceeds along  $H^\dagger H = \frac{\alpha}{\lambda} X^2$

- The Higgs self-coupling  $\lambda$ : must be positive up to inflationary scales

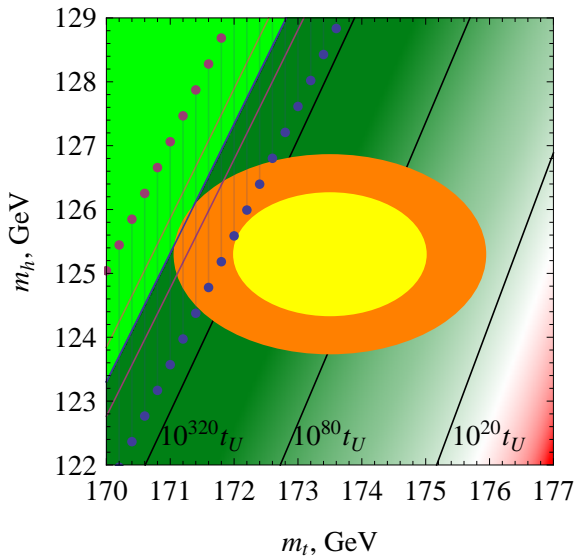


Current experimental value:  $m_H = 125.7 \pm 0.4$  GeV (CMS)

Mass for  $\lambda(\mu) = \beta_\lambda(\mu) = 0$

$$M_{\min} = \left[ 129.5 + \frac{M_t - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \times 1.8 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.6 \pm 2 \right] \text{ GeV}$$

# Critical Higgs mass is compatible with $M_t$ and $\alpha_s$



Vacuum stability

# Conclusions 1: Cosmology

- Single field quartic inflation with *small* non-minimal coupling is perfectly ok with the current CMB observations

## Conclusions 2: Cosmology and Particle Physics

- An example of a model minimally extending SM without any heavy scales: a singlet scalar field with non-minimal coupling
- Cosmological observations constrain the inflaton mass to be light (in GeV range) – interesting for particle physics!
- Further study
  - Detection of tensor modes is especially interesting to constrain the theory
  - The inflaton can be searched in low energy experiments – rare B decays
    - Offset vertices in B decays
    - Peaks in B three body decay Dalitz plot
  - Higgs mass bounds – top quark mass measurement is needed!

# Backup slides

# Dark matter – add $\nu$ MSM and stir

Three Generations  
of Matter (Fermions) spin  $\frac{1}{2}$

	I	II	III	
mass	2.4 MeV	1.27 GeV	171.2 GeV	0
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
name	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon
	Left Right	Left Right	Left Right	0
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon
Quarks	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	Left Right	Left Right	Left Right	0
	$\nu_e$ <b><math>N_1</math></b> electron neutrino sterile neutrino	$\nu_\mu$ <b><math>N_2</math></b> muon neutrino sterile neutrino	$\nu_\tau$ <b><math>N_3</math></b> tau neutrino sterile neutrino	91.2 GeV <b>Z</b> weak force
	$<0.0001$ eV $\sim 10$ keV	$\sim 0.01$ eV $\sim$ GeV	$\sim 0.04$ eV $\sim$ GeV	$>114$ GeV <b>H</b> Higgs boson
	Left Right	Left Right	Left Right	spin 0
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	80.4 GeV $\pm 1$ <b>W</b> weak force
Leptons	-1	-1	-1	$\pm 1$
	Left Right	Left Right	Left Right	

Bosons (Forces) spin 1

## Role of sterile neutrinos

$N_1$  (Warm) Dark Matter,  $M_1 \sim 1\text{--}50$  keV

$N_{2,3}$  Baryogenesis,  $M_{2,3} \sim \dots$  GeV

## Dark matter – add $\nu$ MSM and stir

A  $\nu$ MSM inspired model with inflation  $\chi$

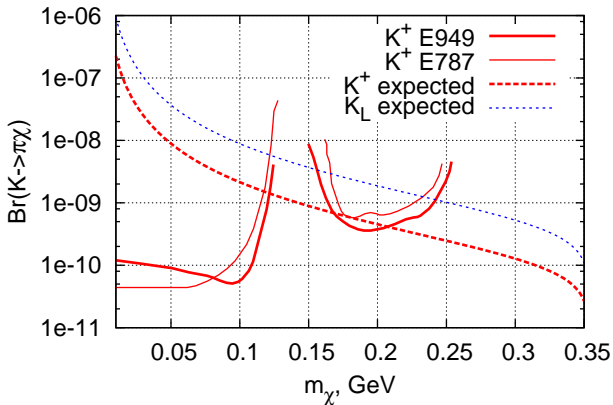
$$\mathcal{L} = (\mathcal{L}_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha l} \bar{L}_\alpha N_I \Phi - \frac{f_I}{2} \bar{N}_I^c N_I X + \text{h.c.}) + \frac{1}{2} (\partial_\mu X)^2 - V(\Phi, X)$$

$$\Omega_N = \frac{1.6 f(m_\chi)}{S} \cdot \frac{\beta}{1.5 \times 10^{-13}} \cdot \left( \frac{M_1}{10 \text{keV}} \right)^3 \cdot \left( \frac{100 \text{MeV}}{m_\chi} \right)^3,$$

### DM sterile neutrino mass bound

$$M_1 \lesssim 13 \cdot \left( \frac{m_\chi}{300 \text{MeV}} \right) \left( \frac{S}{4} \right)^{1/3} \cdot \left( \frac{0.9}{f(m_\chi)} \right)^{1/3} \text{keV}.$$

# Production: bound from $K^+ \rightarrow \pi^+ + \text{nothing}$

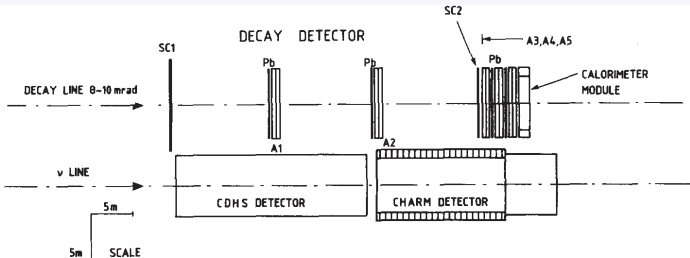


Excluded:  $m_\chi \lesssim 120$  MeV

Disfavoured:  $170 \text{ MeV} \lesssim m_\chi \lesssim 205 \text{ MeV}$



# CHARM – bound

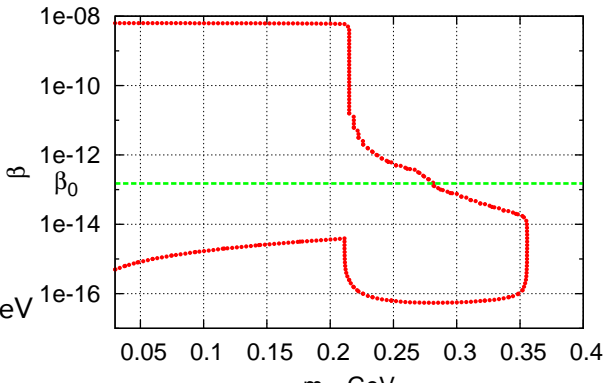


Search for decays of something into

$\gamma\gamma, e^+e^-,$

$\mu^+\mu^- \Rightarrow$

$m_\chi < 270 \text{ MeV}$



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