

Constraining  
Fundamental Physics  
with  
Fundamental Cosmology  
(with three fundamental examples).

MFC2015 Santander

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# Example I: Neutrino Perturbations

# Cosmological Neutrinos

Neutrinos are in equilibrium with the primeval plasma through weak interaction reactions. They decouple from the plasma at a temperature

$$T_{dec} \approx 1MeV$$

We then have today a Cosmological Neutrino Background at a temperature:

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_\gamma \approx 1.945K \rightarrow kT_\nu \approx 1.68 \cdot 10^{-4} eV$$

With a density of:

$$n_f = \frac{3}{4} \frac{\zeta(3)}{\pi^2} g_f T_f^3 \rightarrow n_{\nu_k, \bar{\nu}_k} \approx 0.1827 \cdot T_\nu^3 \approx 112 cm^{-3}$$

That, for a relativistic neutrinos translate in a extra radiation component of:

$$\Omega_\nu h^2 = \frac{7}{4} \left(\frac{4}{11}\right)^{4/3} N_{eff}^\nu \Omega_\gamma h^2$$

Standard Model predicts:

$$N_{eff}^\nu = 3.046$$

# Probing the Neutrino Number with CMB data

Changing the Neutrino effective number essentially changes the expansion rate  $H$  at recombination.

So it changes the sound horizon at recombination:

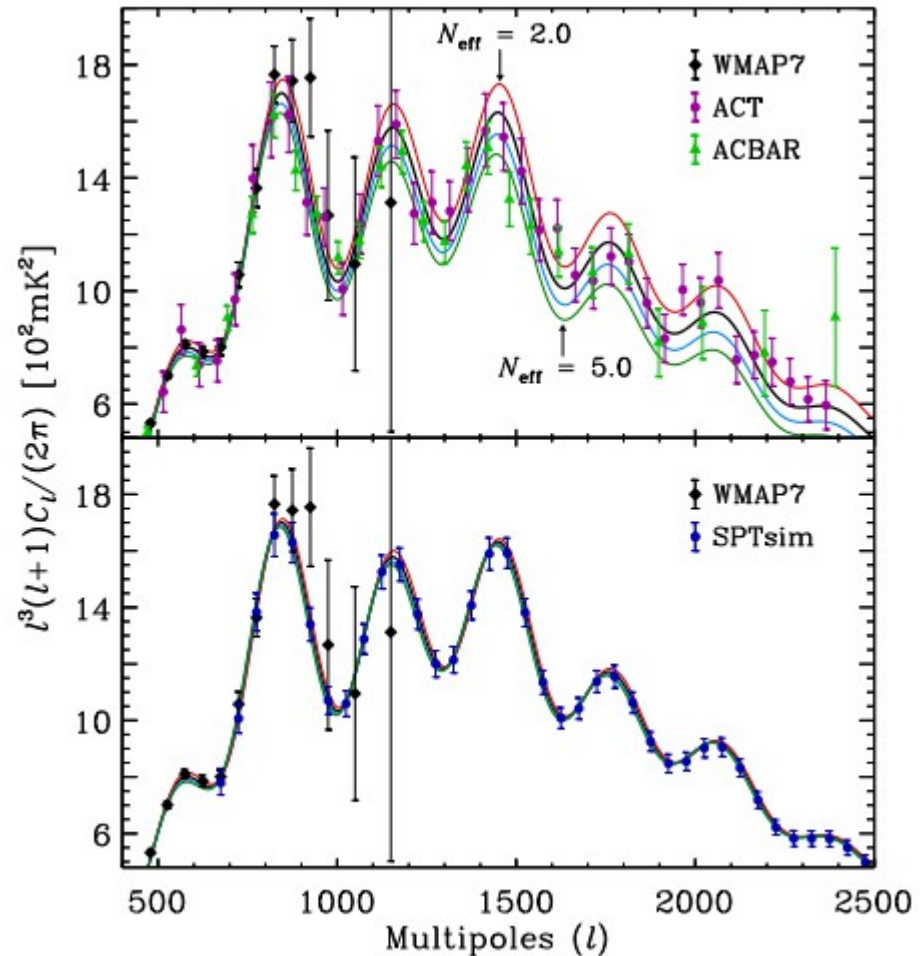
$$r_s = \int_0^{t_*} c_s dt/a = \int_0^{a_*} \frac{c_s da}{a^2 H}$$

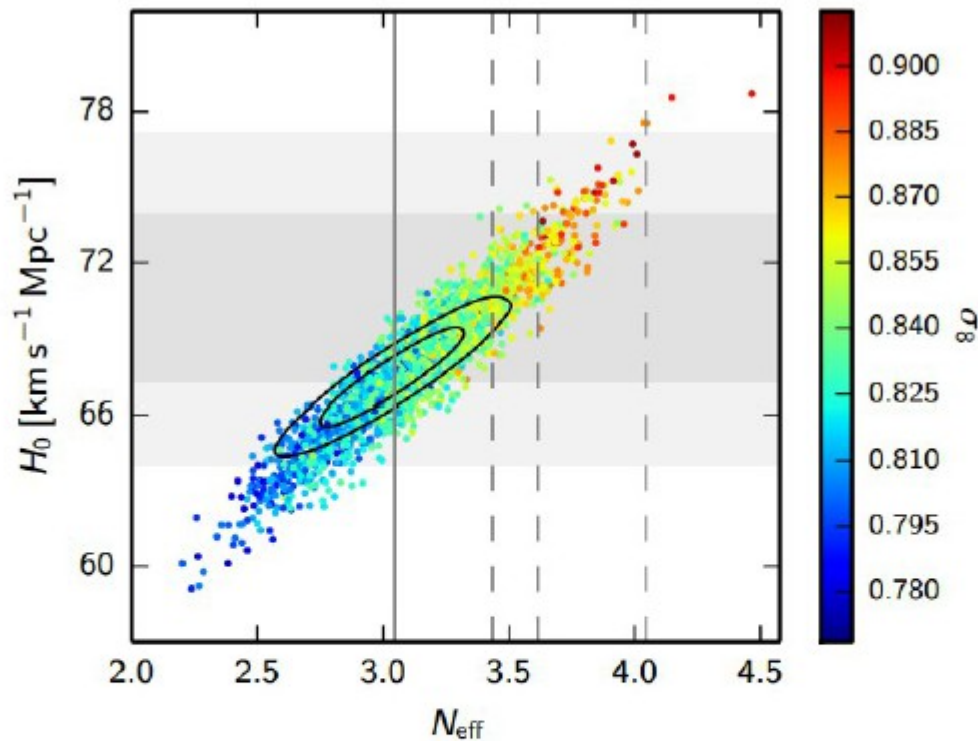
and the damping scale at recombination:

$$r_d^2 = (2\pi)^2 \int_0^{a_*} \frac{da}{a^3 \sigma_T n_e H} \left[ \frac{R^2 + \frac{16}{15} (1 + R)}{6(1 + R^2)} \right]$$

$$\theta_s = \frac{r_s}{D_A} \quad \theta_d = \frac{r_d}{D_A}$$

Moreover increases early ISW at Recombination (phase shift)





Planck 2015 is  
in very good agreement  
with standard  
3 neutrinos  
framework:  
we can further  
test neutrino  
physics

- $N_{\text{eff}} = 3.13 \pm 0.32$  *Planck* TT+lowP;
- $N_{\text{eff}} = 3.15 \pm 0.23$  *Planck* TT+lowP+BAO;
- $N_{\text{eff}} = 2.99 \pm 0.20$  *Planck* TT, TE, EE+lowP;
- $N_{\text{eff}} = 3.04 \pm 0.18$  *Planck* TT, TE, EE+lowP+BAO.

Planck collaboration 2015

Planck “parameters” paper, arXiv:1502.01589, 2015

# Further test: Neutrino Perturbations

Massless neutrinos, like photons, have perturbations and anisotropies which follow a set of differential equations:

$$\dot{\delta}_\nu + k \left( q_\nu + \frac{2}{3k} \dot{h} \right) = \frac{\dot{a}}{a} (1 - 3c_{\text{eff}}^2) \left( \delta_\nu + 3 \frac{\dot{a}}{a} \frac{q_\nu}{k} \right)$$

$$\dot{q}_\nu + \frac{\dot{a}}{a} q_\nu + \frac{2}{3} k \pi_\nu = c_{\text{eff}}^2 \left( \delta_\nu + 3 \frac{\dot{a}}{a} \frac{q_\nu}{k} \right),$$

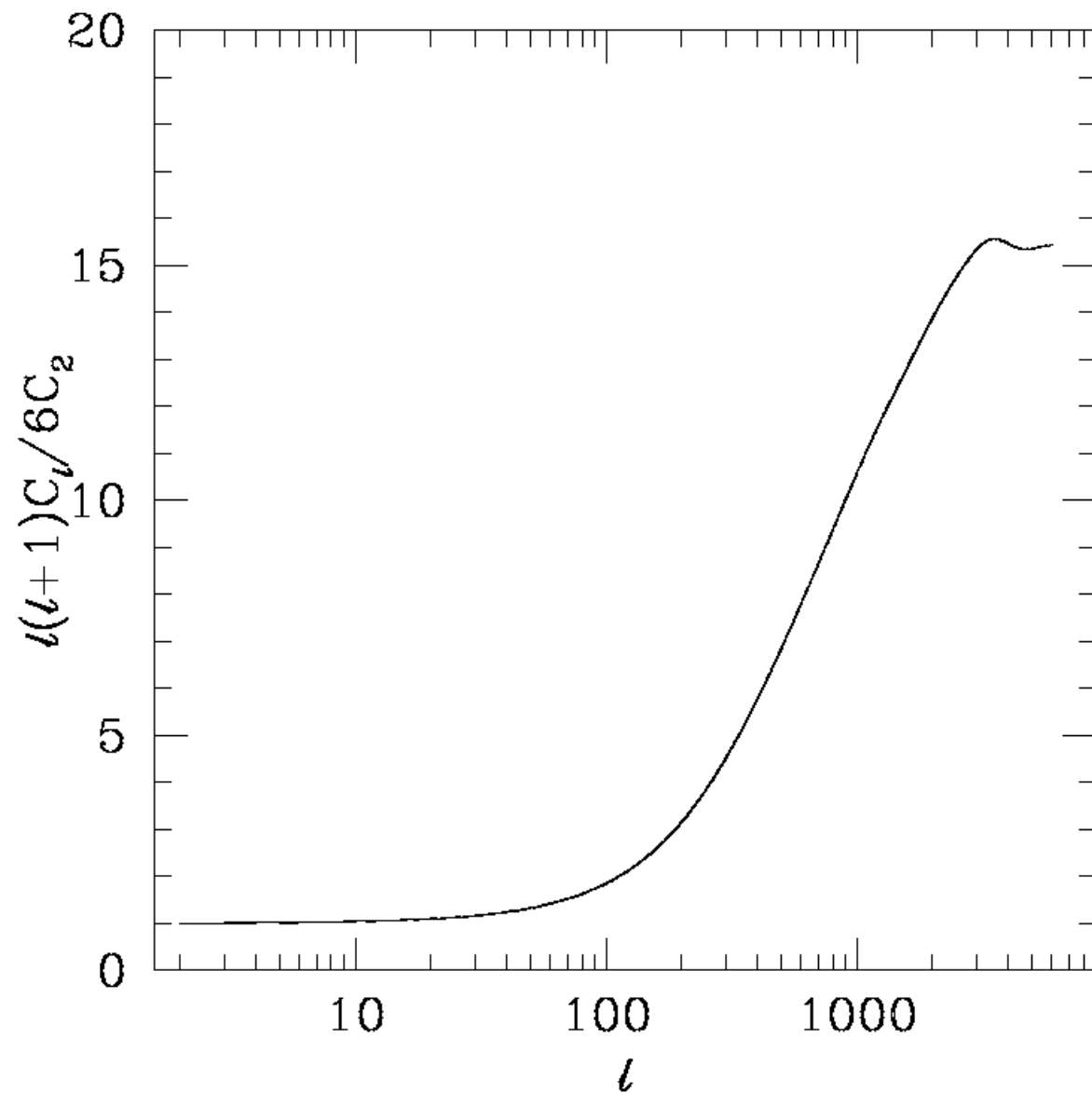
$$\dot{\pi}_\nu + \frac{3}{5} k F_{\nu,3} = 3c_{\text{vis}}^2 \left( \frac{2}{5} q_\nu + \frac{8}{15} \sigma \right),$$

$$\frac{2l+1}{k} \dot{F}_{\nu,l} - l F_{\nu,l-1} = -(l+1) F_{\nu,l+1}, \quad l \geq 3,$$

For the standard massless neutrino case:

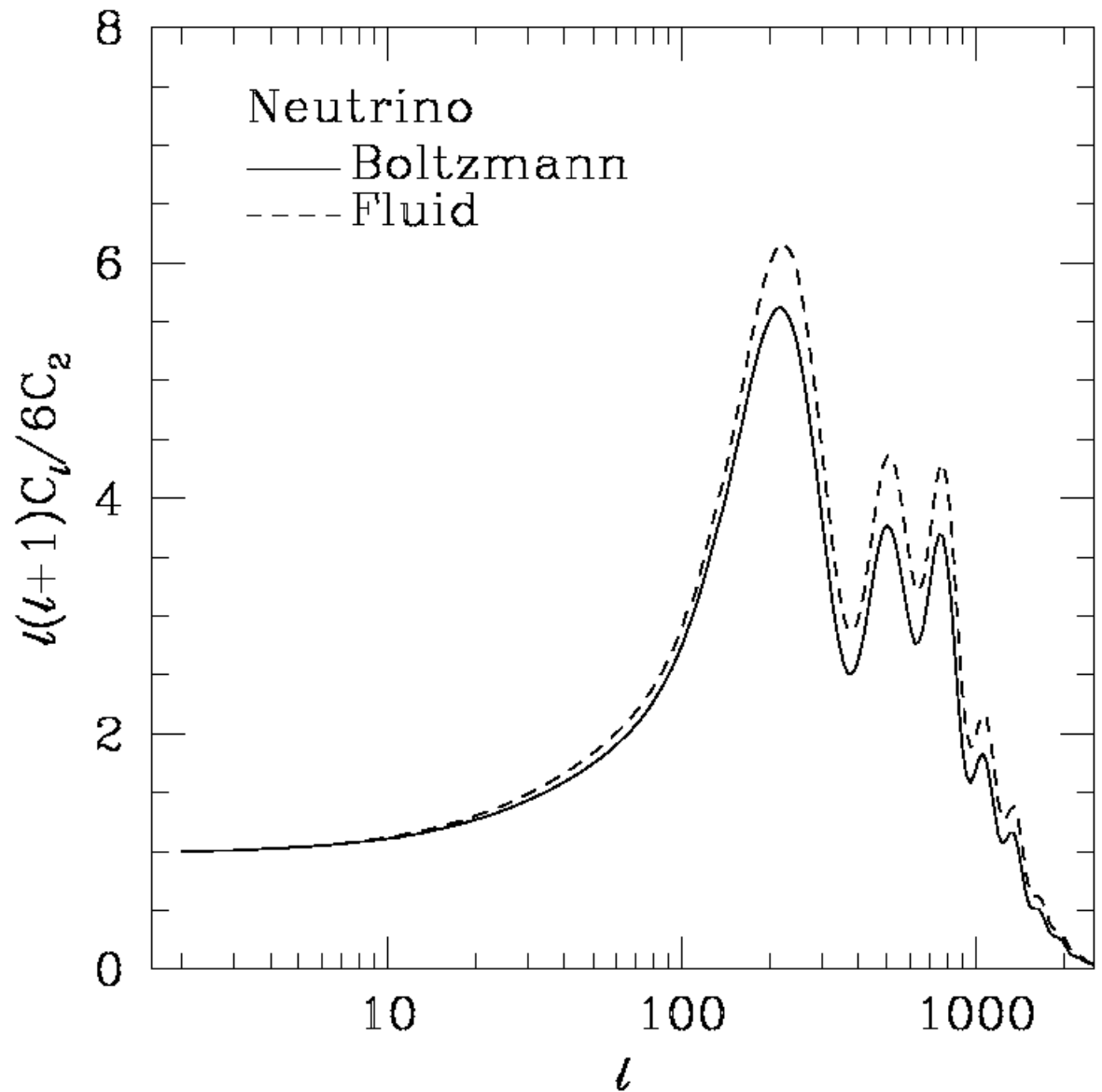
$$c_{\text{eff}}^2 = c_{\text{vis}}^2 = \frac{1}{3}$$

Can we see them ?



Hu et al., astro-ph/9505043

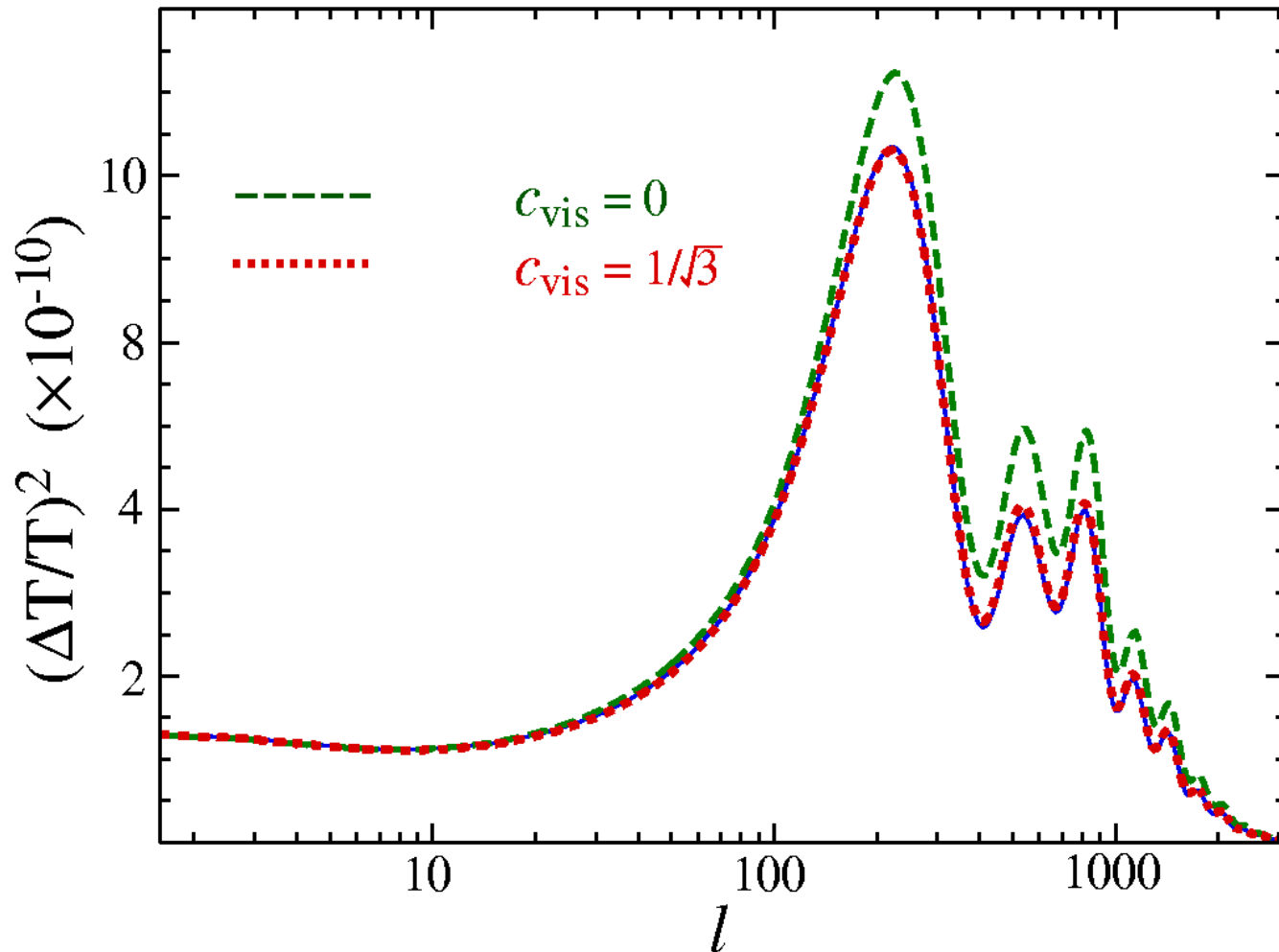
Not directly!  
But we can see the effects on the CMB angular spectrum!  
CMB photons see the NB anisotropies through gravity.



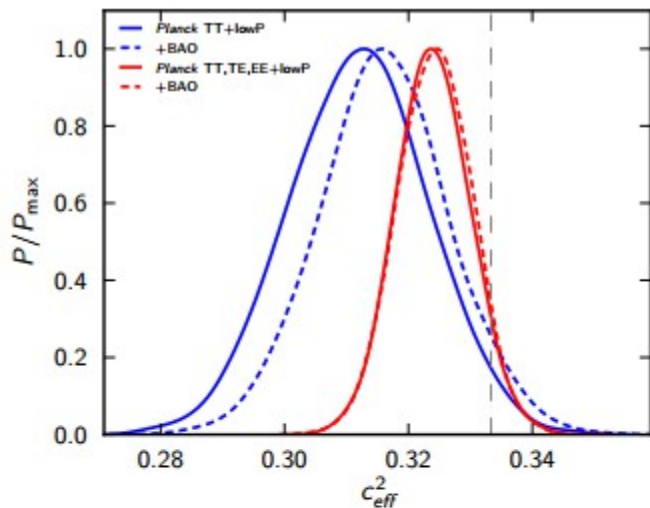
Hu et al., astro-ph/9505043



The Neutrino anisotropies can be parameterized through the “speed viscosity”  $c_{\text{vis}}$ , which controls the relationship between velocity/metric shear and anisotropic stress in the NB.



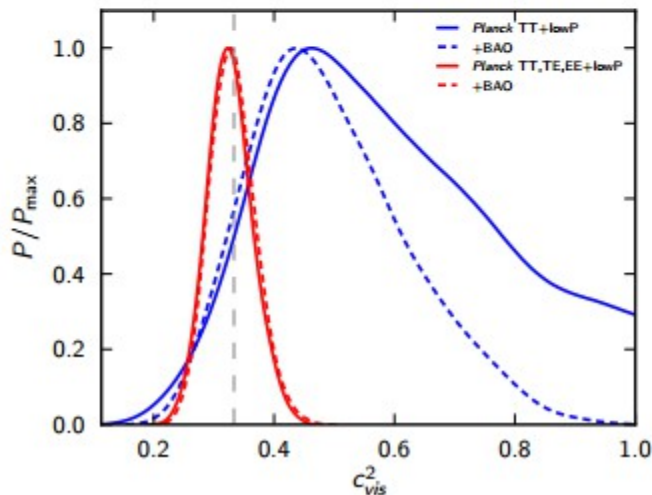
Hu, Eisenstein, Tegmark and White, 1999



$$\left. \begin{aligned} c_{\text{eff}}^2 &= 0.312 \pm 0.011 \\ c_{\text{vis}}^2 &= 0.47^{+0.26}_{-0.12} \end{aligned} \right\} \text{Planck TT+lowP,}$$

$$\left. \begin{aligned} c_{\text{eff}}^2 &= 0.316 \pm 0.010 \\ c_{\text{vis}}^2 &= 0.44^{+0.15}_{-0.10} \end{aligned} \right\} \text{Planck TT+lowP+BAO,}$$

$$\left. \begin{aligned} c_{\text{eff}}^2 &= 0.3240 \pm 0.0060 \\ c_{\text{vis}}^2 &= 0.327 \pm 0.037 \end{aligned} \right\} \text{Planck TT,TE,EE+lowP,}$$

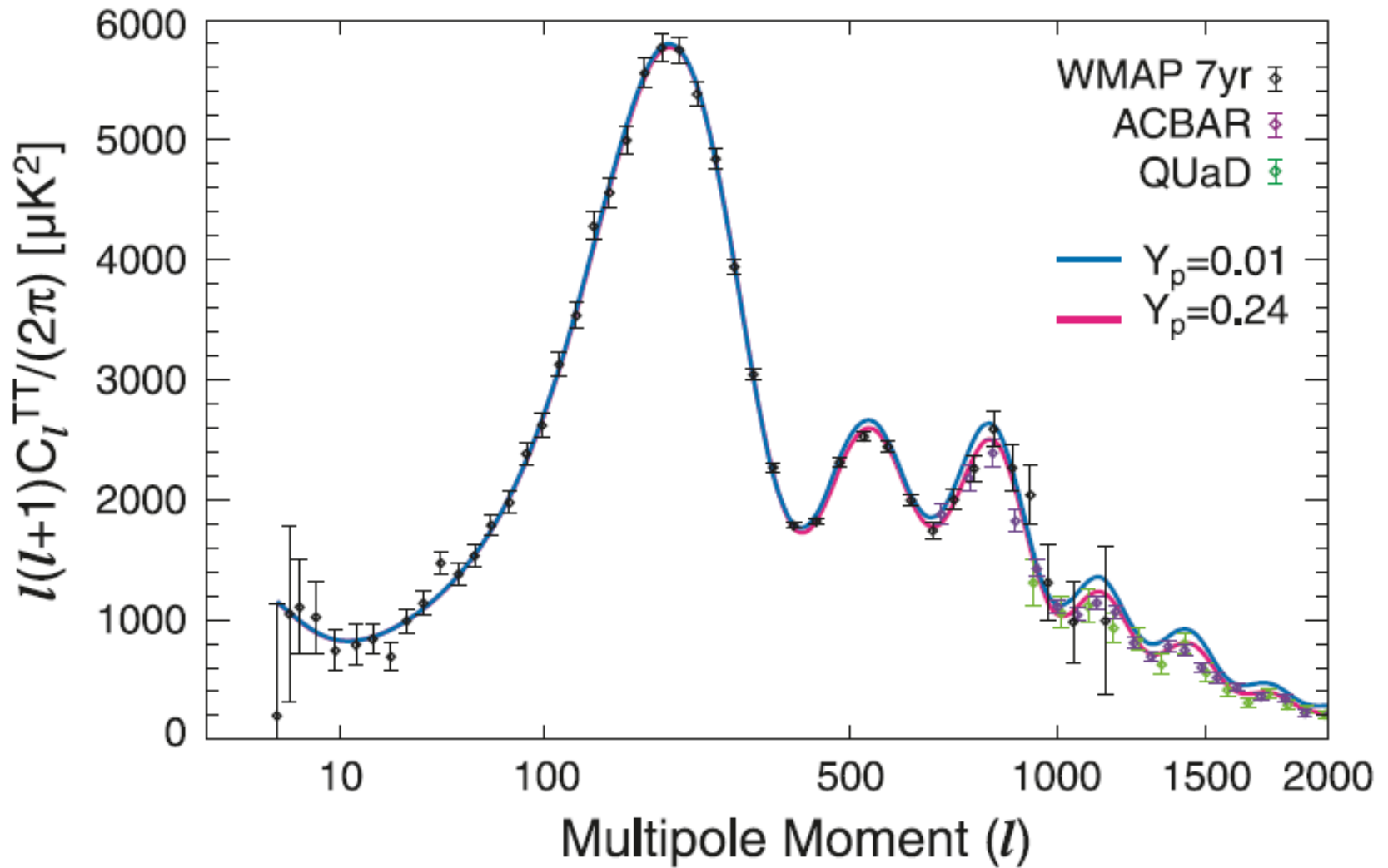


Results consistent with standard model.

Polarization data strongly improves the constraints (by a factor 5 !)

# Example II: BBN and nuclear rates

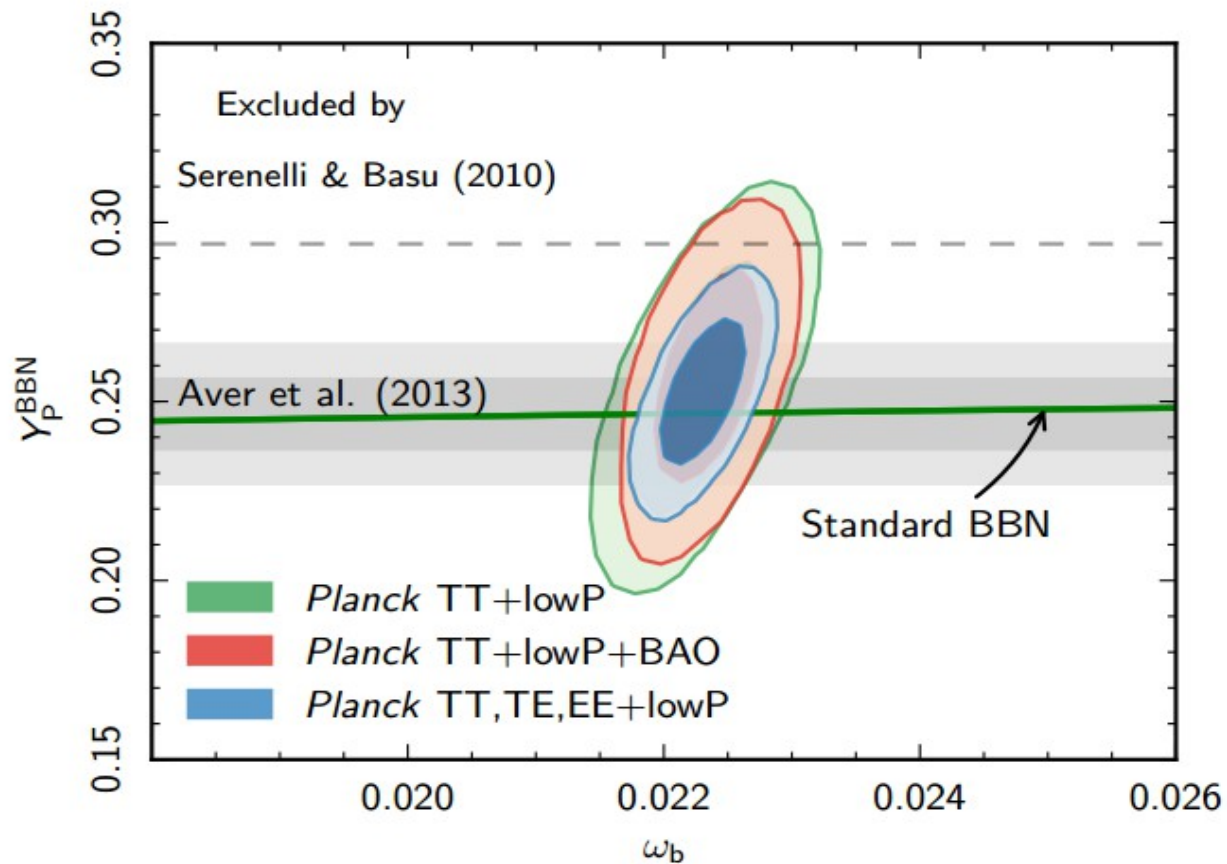
Small scale CMB can probe Helium abundance at recombination.



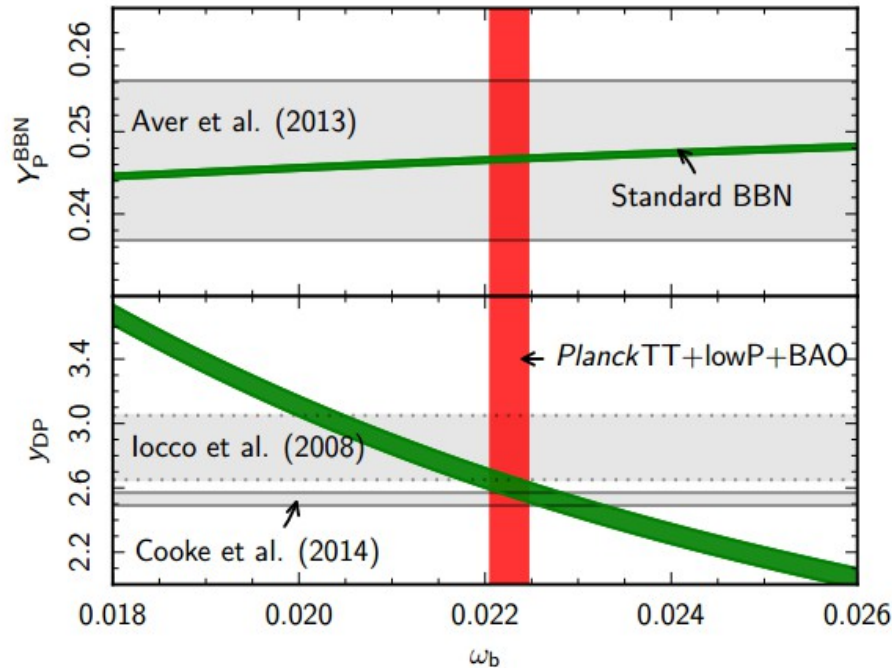
See e.g.,

K. Ichikawa et al., Phys.Rev.D78:043509,2008

R. Trotta, S. H. Hansen, Phys.Rev. D69 (2004) 023509



$$Y_P^{BBN} = \begin{cases} 0.253^{+0.041}_{-0.042} & \text{Planck TT+lowP;} \\ 0.255^{+0.036}_{-0.038} & \text{Planck TT+lowP+BAO;} \\ 0.251^{+0.026}_{-0.027} & \text{Planck TT,TE,EE+lowP;} \\ 0.253^{+0.025}_{-0.026} & \text{Planck TT,TE,EE+lowP+BAO.} \end{cases}$$



Abundances can also be derived indirectly by combining CMB observations of the baryon density with standard BBN codes.

Planck determination of the baryon density is now so precise that uncertainties in BBN rates (i.e. neutron lifetime for Helium) have a major impact !

$$Y_P^{BBN} = \begin{cases} 0.24665^{+(0.00020) 0.00063}_{-(0.00019) 0.00063} & \text{Planck TT+lowP,} \\ 0.24667^{+(0.00018) 0.00063}_{-(0.00018) 0.00063} & \text{Planck TT+lowP+BAO,} \\ 0.24667^{+(0.00014) 0.00062}_{-(0.00014) 0.00062} & \text{Planck TT,TE,EE+lowP,} \\ 0.24668^{+(0.00013) 0.00061}_{-(0.00013) 0.00061} & \text{Planck TT,TE,EE+lowP+BAO,} \end{cases}$$

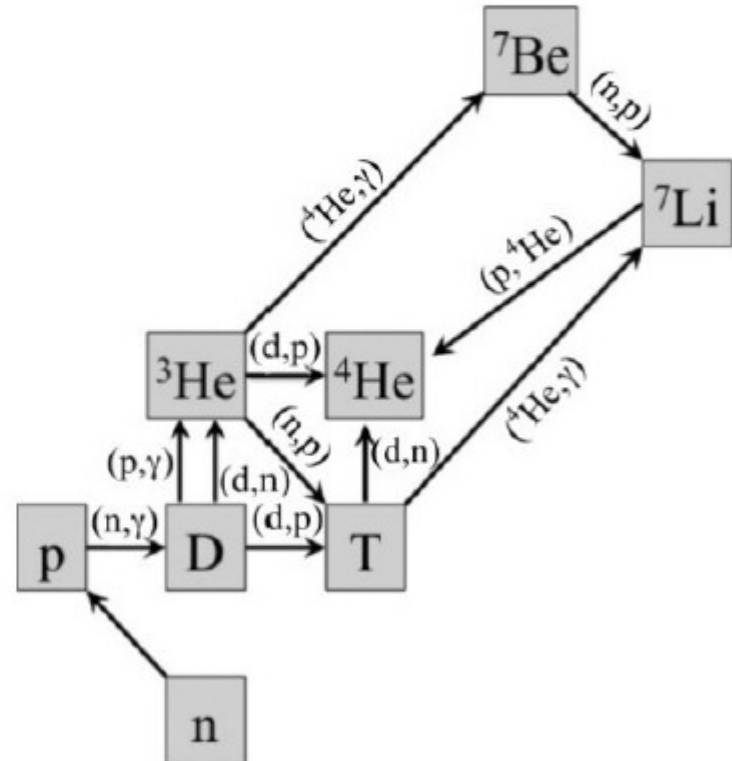
$$Y_{DP} = \begin{cases} 2.620^{+(0.083) 0.15}_{-(0.085) 0.15} & \text{Planck TT+lowP,} \\ 2.612^{+(0.075) 0.14}_{-(0.074) 0.14} & \text{Planck TT+lowP+BAO,} \\ 2.614^{+(0.057) 0.13}_{-(0.060) 0.13} & \text{Planck TT,TE,EE+lowP,} \\ 2.606^{+(0.051) 0.13}_{-(0.054) 0.13} & \text{Planck TT,TE,EE+lowP+BAO.} \end{cases}$$

# $d(p;\gamma)^3\text{He}$

The main uncertainty for standard BBN calculations of  $^2\text{H}$  comes from the rate  $R_2$  of the radiative capture reaction  $d(p;\gamma)^3\text{He}$ , measured from nuclear experimental data.

Reaction	Rate Symbol	$\sigma_{^2\text{H}/\text{H}} \cdot 10^5$
$p(n,\gamma)^2\text{H}$	$R_1$	$\pm 0.002$
$d(p,\gamma)^3\text{He}$	$R_2$	$\pm 0.062$
$d(d,n)^3\text{He}$	$R_3$	$\pm 0.020$
$d(d,p)^3\text{H}$	$R_4$	$\pm 0.013$

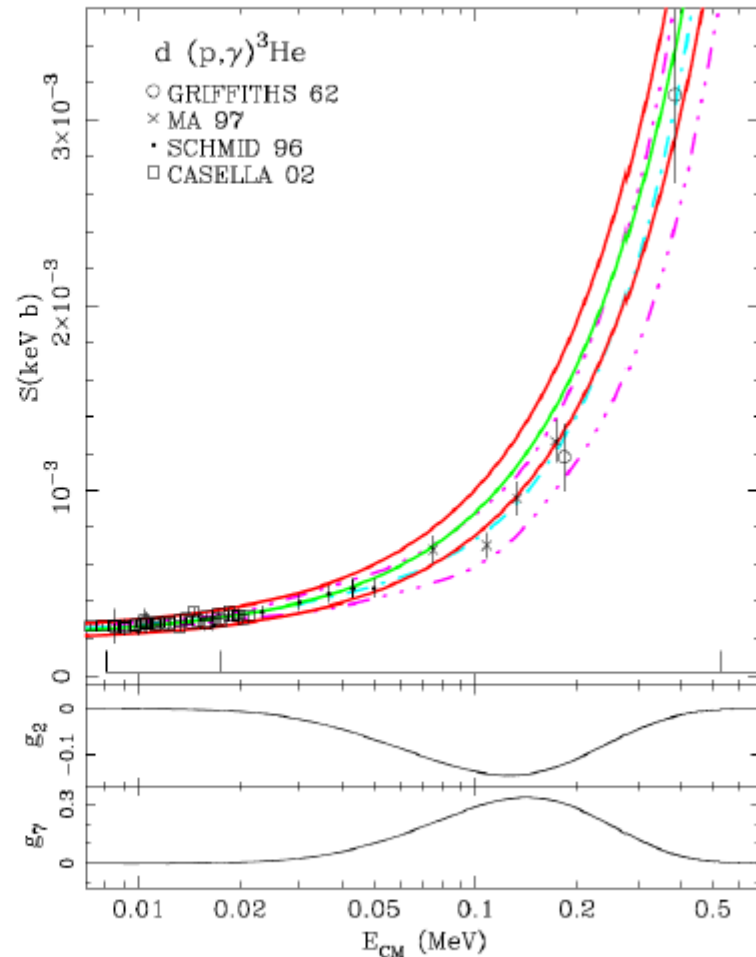
TABLE I: List of the leading reactions and corresponding rate symbols controlling the deuterium abundance after BBN. The last column shows the error on the ratio  $^2\text{H}/\text{H}$  coming from experimental (or theoretical) uncertainties in the cross section of each reaction, for a fixed baryon density  $\Omega_b h^2 = 0.02207$ .



# $d(p,\gamma)^3\text{He}$

The main uncertainty for standard BBN calculations of  $^2\text{H}$  comes from the rate  $R_2$  of the radiative capture reaction  $d(p,\gamma)^3\text{He}$ , measured from nuclear experimental data.

A reliable *ab initio* nuclear theory calculation of this cross section is systematically larger than the best-fit value derived from the experimental data in the BBN energy range [30-300 keV]. Further data on  $R_2$  in the relevant energy range might be expected from experiments such as LUNA.

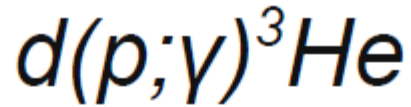




Assuming the standard cosmological model, following E. Di Valentino et al., Phys. Rev. D90 (2014), 023543, we can combine

- the Planck data
- the direct deuterium abundance measurements in metal-poor damped Lyman-alpha systems

and have independent information on the cross section of the radiative capture reaction  $d(p;\gamma)^3\text{He}$  converting deuterium into helium.



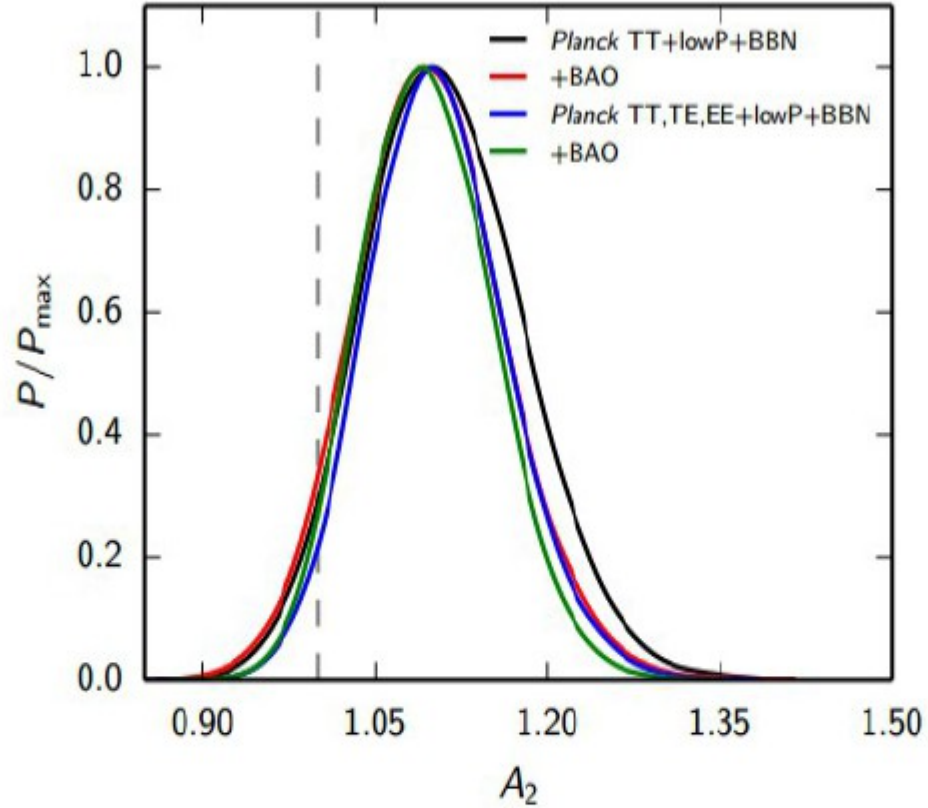
We analyzed the Planck data considering the rate of the radiative capture reaction  $d(p;\gamma)^3\text{He}$  as a free input parameter.

Actually the present CMB data (combined with primordial D measurements) are powerful enough to provide information on nuclear rates.

We find that our results give independent support to the theoretical calculation: the rate of the radiative capture reaction  $d(p;\gamma)^3\text{He}$  is larger than measured from the nuclear experiments.

We parametrize the generic  $R_2(T)$  in terms of an overall rescaling factor  $A_2$

$$R_2(T) = A_2 R_2^{ex}(T)$$



$A_2 = 1.106 \pm 0.071$  *Planck* TT+lowP ,  
 $A_2 = 1.098 \pm 0.067$  *Planck* TT+lowP+BAO ,  
 $A_2 = 1.110 \pm 0.062$  *Planck* TT, TE, EE+lowP ,  
 $A_2 = 1.109 \pm 0.058$  *Planck* TT, TE, EE+lowP+BAO .

# Example III: Dark Matter Annihilation

The rate of energy release per unit volume from annihilating Dark Matter is given By (see Chen and Kamionkowski 2004):

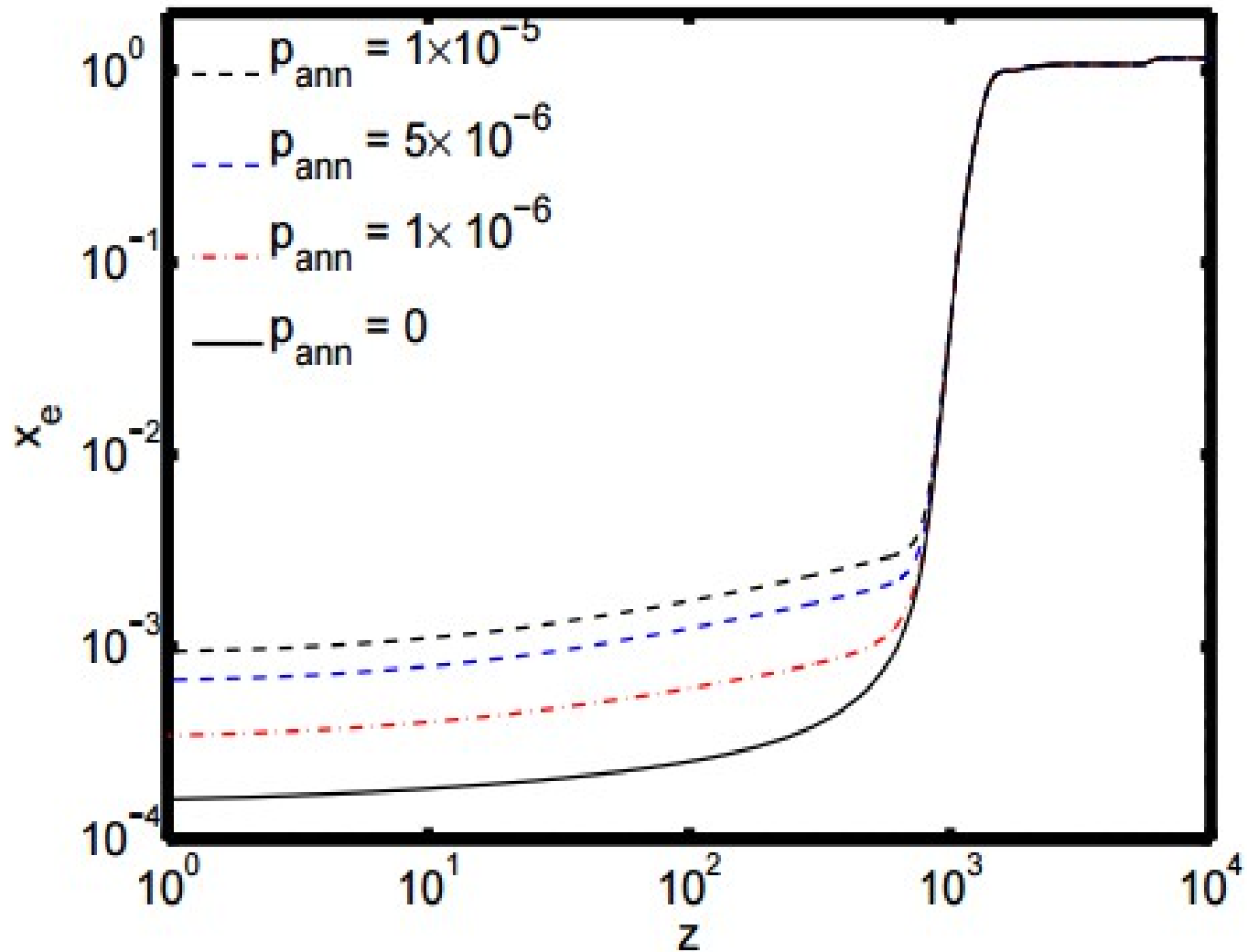
$$\frac{dE}{dt} = \rho_c^2 c^2 \Omega_{DM}^2 (1+z)^6 f(z) \frac{\langle \sigma v \rangle}{m_\chi}$$

Where  $\rho_c$  is the critical density of the Universe today,  $\Omega_{DM}$  is the density of cold dark matter today,  $\langle \sigma v \rangle$  is the thermally averaged cross section of self-annihilating dark matter,  $m_\chi$  is the dark matter mass,  $f(z)$  is the fraction of the overall annihilation energy absorbed by the medium (ionization, Lyman-alpha, heating).

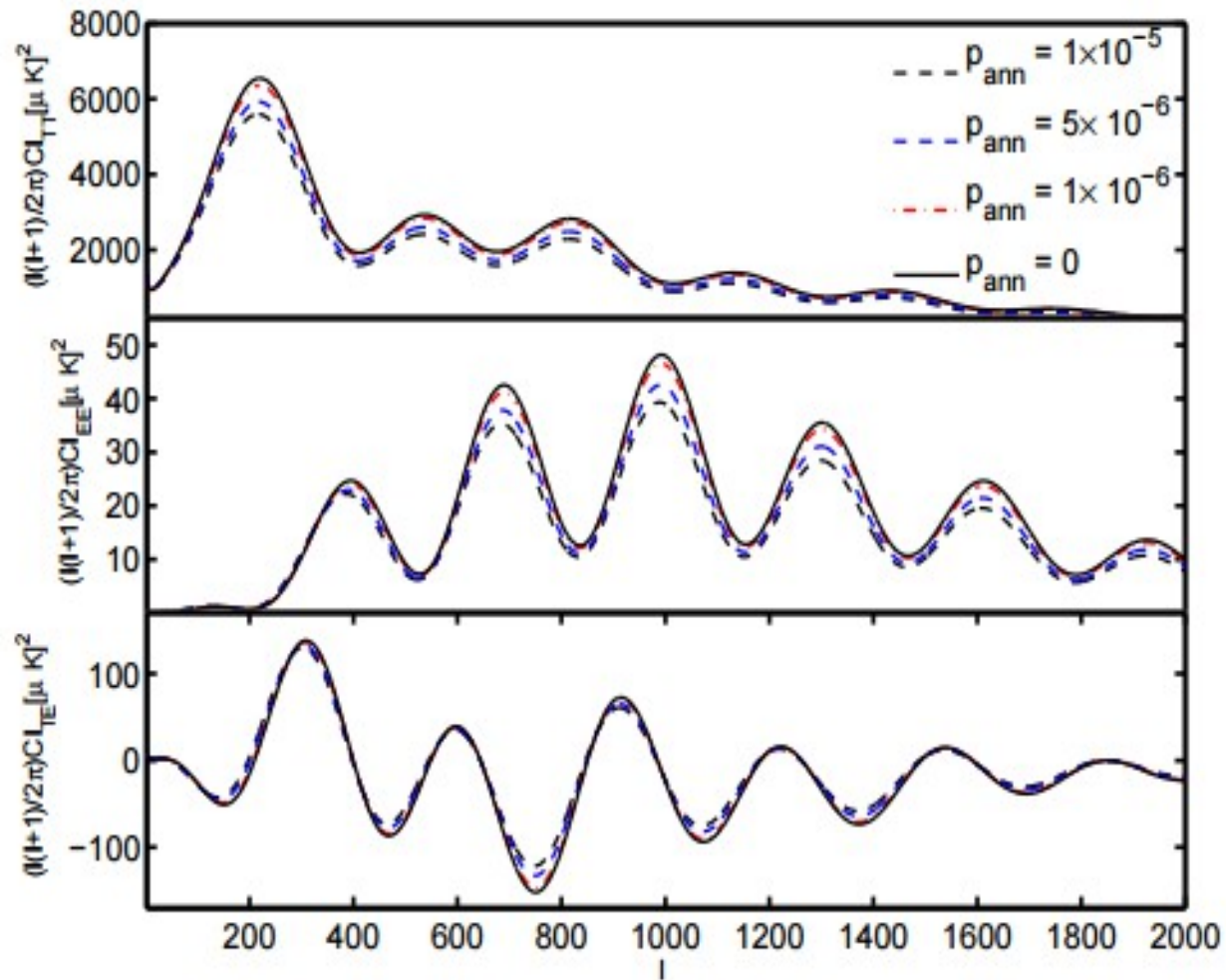
We assume  $f(z)$  constant with redshift with  $f(z) = f_{eff}$ .

The whole DM annihilation process can be parametrized by a single parameter:

$$P_{ann} = f_{eff} \frac{\langle \sigma v \rangle}{m_\chi}$$

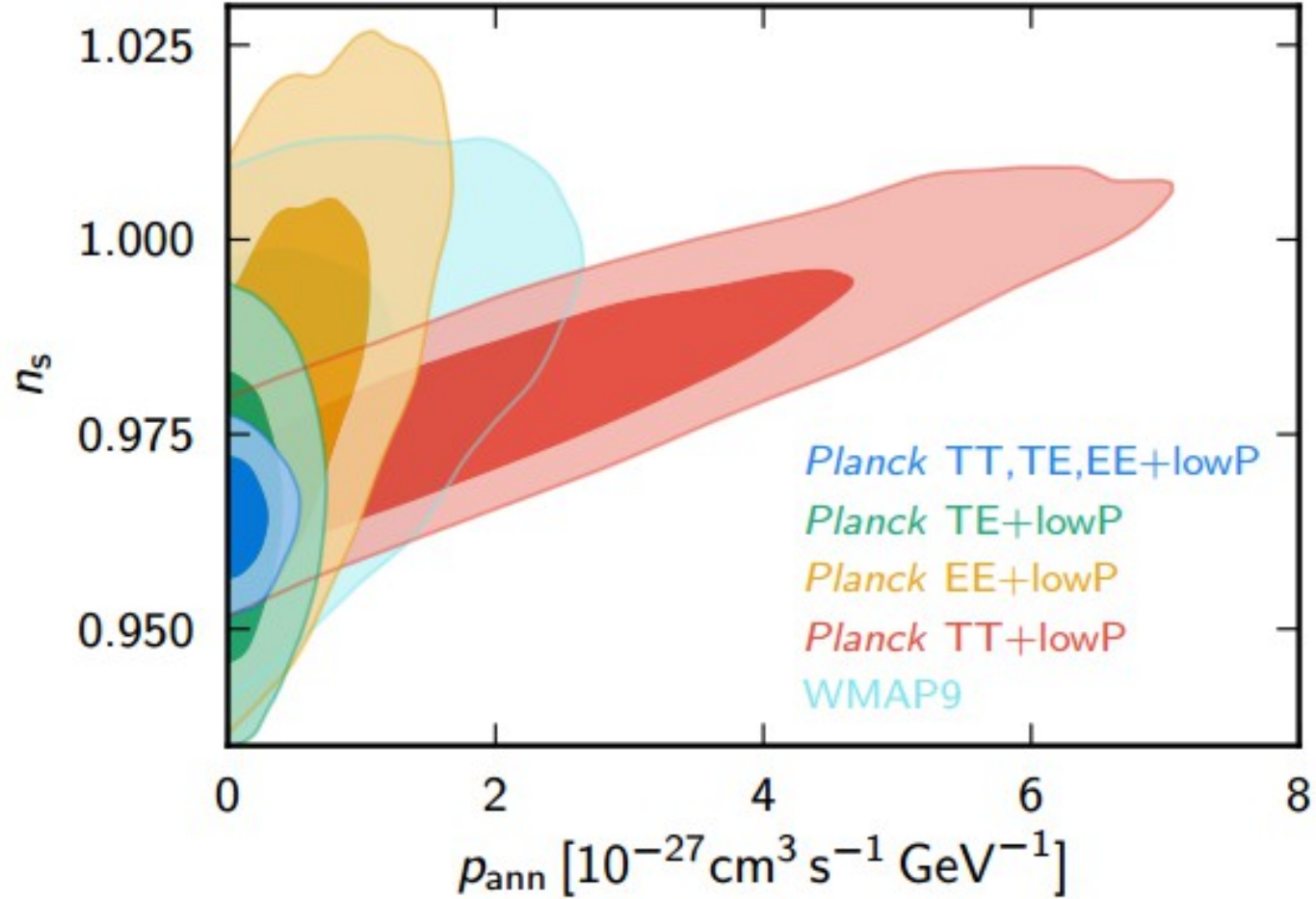


DM annihilation heats, ionizes and excites the primordial plasma leading to a delayed recombination...

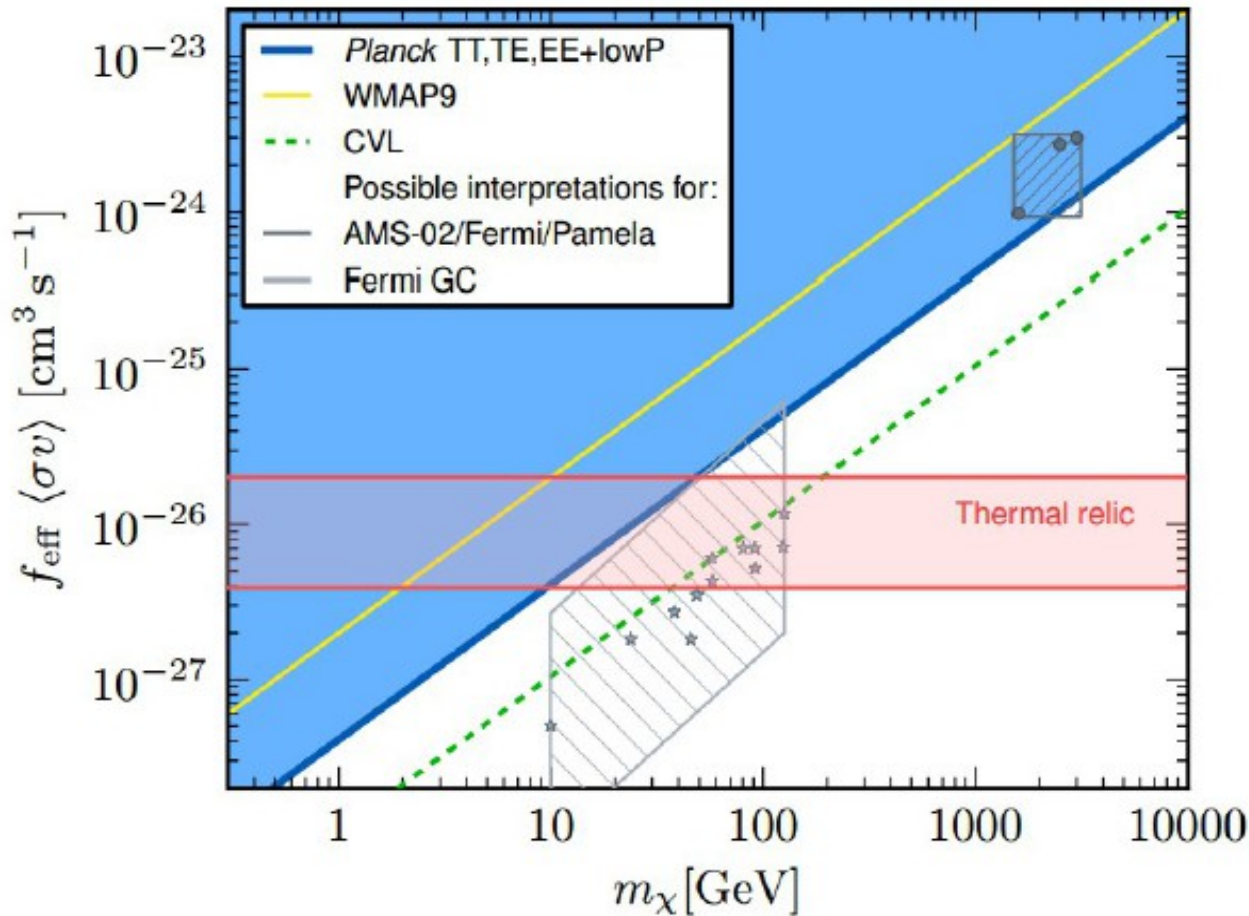


...and to a change in the positions and amplitudes of the CMB peaks.

See e.g. Bean et al, 2007, Galli et al 2009, Galli et al 2011.







Most of parameter space preferred by AMS-02/Pamela/Fermi ruled out at 95%, under the assumption  $\langle \sigma v \rangle(z=100) = \langle \sigma v \rangle(z=0)$  (s-wave annihilation)

In case of Sommerfeld enhancement  $\langle \sigma v \rangle \sim 1/v$  so constraints can be even stronger for today !

For p-wave annihilation  $\langle \sigma v \rangle \sim v^2$  and constraints “today” are weaker.

**The scientific results that we present today are a product of the Planck Collaboration, including individuals from more than 100 scientific institutes in Europe, the USA and Canada.**



Planck is a project of the European Space Agency, with instruments provided by two scientific Consortia funded by ESA member states (in particular the lead countries: France and Italy) with contributions from NASA (USA), and telescope reflectors provided in a collaboration between ESA and a scientific Consortium led and funded by Denmark.